

Strand 2 Chapter 2 Trigonometry

1. I know that a radian is the measure of the angle at the centre of a circle subtended by an arc equal in length to the radius.
2. I know that π radians = 180° and that 1 radian = 57.3°
3. I can convert from radians to degrees and from degrees to radians.

Example 1 Page 35

4. I can find the Arc Length ($l = r\theta$) and the Area of Sector ($A = \frac{1}{2} r^2\theta$) using formulae.

Example 2 Page 35**Ex 2.1 Q1 – Q15 Odd Page 35**

5. I am aware of the trigonometric ratios sin, cos and tan as well as the other ratios **Secant** ($\sec\theta = 1/\cos\theta$), **Cosecant** ($\operatorname{cosec}\theta = 1/\sin\theta$) and **Cotangent** ($\cot\theta = 1/\tan\theta$)
6. Given tan B, I can draw a rough sketch of a right angled triangle to find sin b and cos b

Example 1 Page 38

7. I can use my calculator to find the sin, cos or tan of an angle.
8. I can use the $^{\circ}$ button on my calculator to perform calculations in degrees, minutes and seconds.

Example 2 Page 39

9. Given the tan, cos or sin value of an angle θ , I can find the angle θ using the \sin^{-1} , \cos^{-1} and \tan^{-1} inverse
10. I know that the sin, cos and tan of the angles 30° , 45° and 60° are often expressed as fractions or surds which can be found on page 13 of the *Formulae and Tables*.
11. I know that $(\sin^2\theta) = (\sin\theta)(\sin\theta)$

Ex 2.2 Q2 – Q8 Even Page 40

12. I know that positive angles are measured anticlockwise from the +ve x-axis
13. I know that negative angles are measured in a clockwise direction.
14. I know that the coordinates of any point P on the Unit circle (radius = 1 unit) are **(cos θ sin θ)**
15. I know that a circle has 4 quadrants and that the **CAST Rule** is used to determine if the trig ratio of an angle between 0° and 360° is positive or negative.
16. I know that reference angles are measured in each quadrant are measured from the x axis and that the **trig ratio of a reference angle is = the trig ratio of its corresponding larger angle**

i.e. to find $\sin 120^\circ$... Find the reference angle = $180^\circ - 120^\circ = 60^\circ$ and then note the sin of the trig ratio for the reference angle in the 2nd quadrant (it is positive)

Therefore $\sin 120^\circ = \sin 60^\circ = \sqrt{3}/2$

17. I know that two different angles can have the same sin, cos or tan trig ratio value.

18. I can express in surd form the sin, cos or tan of angles between 90° and 360°

19. Given a value for $\sin x$, I can find 2 values for x if $0^\circ < x < 360^\circ$

Example 1 and 2 Page 42

Ex 2.3 Q1 – Q17 Odd Page 43

20. I know to use A, B, C to denote angles and a, b and c to denote the sides opposite these angles.

21. Given one side and the angle opp this side and one other side or angle I know how to use the **Sine Rule** to solve a non right angled triangle.

Example 1 and 2 Page 45

22. I know that 2 possible triangles can be drawn (ambiguous case) when given 2 sides and a non included angle. (See page 46)

Example 3 Page 47

23. I know how to find the area of a triangle using **area = half the product of any 2 sides multiplied by the sine of the angle between them**

Example 4 Page 47

Ex 2.4 Q2 – Q12 Even Page 48

24. I know that if I am presented with a triangle of **3 known sides and no angle** that I can solve the non right angled triangle using the **cosine rule**

Example 1 and Example 2 Page 51

2.5 Q1 – Q13 Odd Page 52

25. I know the importance of sketching good 3d diagrams.

26. I know the importance of looking for connected and right angled triangles in 3d diagrams/sketches

Example 1 Example 2 Example 3 Page 54

Ex 2.6 Q2 – Q12 Even Page 57

27. I know that a graph of $y = \sin x$ for $0^\circ < x < 360^\circ$ has a **Period (repeats itself) of 360°** (or 2π radians) and has a **range of $[-1, 1]$**

28. I know that a graph of $y = \cos x$ for $0^\circ < x < 360^\circ$ has a **Period (repeats itself) of 360°** (or 2π radians) and has a **range of $[-1,1]$**
29. I know that a graph of $y = \tan x$ for $0^\circ < x < 360^\circ$ behaves differently to sin and cos and has a **Period (repeats itself) of 180°** (or π radians) and has **vertical asymptotes** (lines that the tangent curve approaches but never touches) which are **undefined at $x=90^\circ$ and $x=270^\circ$**
30. I can draw any of the above graphs and can show the angles which satisfy given equations.

Example 1 Page 62

31. I know that a graph of $y = a \sin nx$ has a **period $2\pi/n$**
32. I know that a graph of $y = a \cos nx$ has a **period $2\pi/n$**
33. I know that a graph of $y = a \sin nx$ has **range $[-a,a]$**
34. I know that a graph of $y = a \cos nx$ has **range $[-a,a]$**

Example 2 Page 64**Ex 2.7 Q2 – Q12 Even Page 64**

35. I know that a calculator in degree mode will tell me that for **$\cos \theta = \frac{1}{2}$ that $\theta = 60^\circ$** but that there are other angles which satisfy this trigonometric equation (from CAST Rule Section) like 300° and 420° and that there is no restriction on the values of θ that are solutions.
36. I know that I can plot $y = \cos \theta$ and $y = \frac{1}{2}$ to solve $\cos \theta = \frac{1}{2}$ See Page 67
37. I know that to find the General Solution of an equation like **$\sin x = k$ or $\cos x = k$ that you find the 2 solutions in the interval $0^\circ < x < 360^\circ$ and then add $n360^\circ$ to each of the solutions**
38. I know that to solve the equation $\sin 3x = k$, to first find the general solution for the angle $3x$ and then divide both parts by 3 to find the general solution for x
See Examples 1, 2 and 3 Pages 68
39. I know that for $\tan x = k$ because the tangent curve has a period of π , that we find a value of x in the interval 0 to π and then add $n\pi$ to this to give the general solution.
Ex 2.8 Q2 – Q14 Page 70